

UNIT 5 STUDENT PACKET

Implicit Differentiation Practice

Find $\frac{dy}{dx}$.

1. $\sin(y) + xy^3 = 3x$

$$\cos(y) \frac{dy}{dx} + x \cdot 3y^2 \frac{dy}{dx} + y^3 = 3$$

$$\frac{dy}{dx} = \frac{3 - y^3}{\cos(y) + 3xy^2}$$

2. $[4x^2y^3 + 3xy^3] = 2x$

$$4x^2 \cancel{3y^2} \frac{dy}{dx} + \cancel{8x} \cancel{y^3} + \cancel{y^9} x^2 + \frac{dy}{dx} (3x^3) = 2$$

$$\frac{dy}{dx} = \frac{2 - 8xy^3 - 9x^2y}{4x^2 3y^2 + 3x^3}$$

$$12x^2y^4$$

3. $xy + e^{2y+1} = 2x$

$$x \frac{dy}{dx} + y + e^{2y+1} \cdot 2 \frac{dy}{dx} = 2$$

$$\frac{dy}{dx} = \frac{2-y}{x+2e^{2y+1}}$$

4. $y^3 + xy = 3y$

$$3y^2 \frac{dy}{dx} + x \frac{dy}{dx} + y = 3 \frac{dy}{dx}$$

$$\frac{dy}{dx} = \frac{-y}{3y^2 + x - 3}$$

Find $\frac{d^2y}{dx^2}$.

5. $2y - 3x^2 = xy$

$$y+6x$$

$$\frac{dy}{dx} = \frac{y+6x}{2-x}$$

$$2 \frac{dy}{dx} - 6x = x \frac{dy}{dx} + y$$

$$\frac{(2-x)(6 + \frac{y+6x}{2-x}) + (y+6x)}{(2-x)^2}$$

$$\frac{(2-x)(6 + \frac{dy}{dx}) - (y+6x)(-1)}{(2-x)^2}$$

$$\frac{(2-x)(6 + \frac{y+6x}{2-x}) + (y+6x)}{(2-x)^2}$$

6. Find the equations of the tangent and normal line to the curve $xy^2 = 16$ at $(1, 4)$.

tangent $y - 4 = -2(x - 1)$

normal $y - 4 = \frac{1}{2}(x - 1)$

$$x \cdot 2y \frac{dy}{dx} + y^2 = 0$$

$$1 \cdot 2(4) \frac{dy}{dx} + 4^2 = 0$$

$$8 \frac{dy}{dx} + 16 = 0$$

$$-16 = -8 \frac{dy}{dx}$$

$$-2 = \frac{dy}{dx}$$