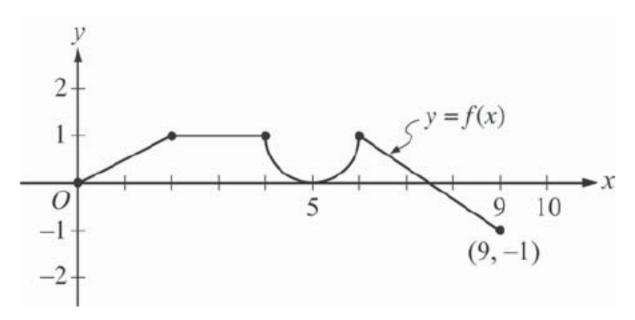
## I.5 Integrals and Integral Properties



$$1. \int_4^0 f(t)dt$$

$$2. \int_0^6 f(t)dt$$

$$3. \int_4^2 f(t)dt$$

$$4. \int_2^0 2f(t)dt$$

5. 
$$\int_0^4 [f(t) + 2]dt$$

$$6. \int_8^8 f(t)dt$$

$$7. \int_{6}^{9} [3f(t) - 1]dt$$

$$8. \int_6^9 |f(t)| dt$$

9. Major Integral Rules:

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Suppose 
$$\int_{-2}^{5} f(x) dx = 18$$
,  $\int_{-2}^{5} g(x) dx = 5$ ,  $\int_{-2}^{5} h(x) dx = -11$  and  $\int_{-2}^{8} f(x) dx = 0$ , find

10. 
$$\int_{-2}^{5} (f(x) + g(x)) dx$$

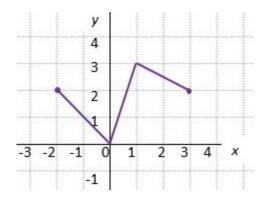
11. 
$$\int_{-2}^{5} (f(x) - h(x)) dx$$

12. 
$$\int_{5}^{-2} 4g(x)dx$$

13. 
$$\int_{-2}^{5} (2g(x) + 2) dx$$

14. If f(-1) = 2 and the graph of f', the derivative of f, is given below, what is the value of f(3)?

f'

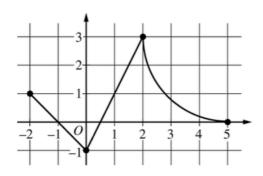


15. The average value of function g on the interval  $3 \le x \le 9$  is 7. What is the value of  $\int_3^9 g(x)dx$ ?

Average value:

## INTERVENTION STUDENT PACKET

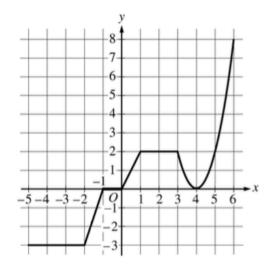
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Graph of f

- 3. The continuous function f is defined on the closed interval  $-6 \le x \le 5$ . The figure above shows a portion of the graph of f, consisting of two line segments and a quarter of a circle centered at the point (5, 3). It is known that the point  $(3, 3 \sqrt{5})$  is on the graph of f.
  - (a) If  $\int_{-6}^{5} f(x) dx = 7$ , find the value of  $\int_{-6}^{-2} f(x) dx$ . Show the work that leads to your answer.
  - (b) Evaluate  $\int_{3}^{5} (2f'(x) + 4) dx$ .

BC 2018 #3



Graph of g

- 3. The graph of the continuous function g, the derivative of the function f, is shown above. The function g is piecewise linear for  $-5 \le x < 3$ , and  $g(x) = 2(x-4)^2$  for  $3 \le x \le 6$ .
  - (a) If f(1) = 3, what is the value of f(-5)?
  - (b) Evaluate  $\int_1^6 g(x) dx$ .