

**Station 1: Inverses and Functions**

Let  $f(x) = 9 - x$ ,  $g(x) = x^2 + x$ , and  $h(x) = x - 2$ . Compute the following:

10.  $g(f(3))$

$$f(3) = 9 - 3 = 6$$
$$g(6) = 6^2 + 6 = \textcircled{42}$$

11.  $f(g(4))$

$$g(4) = 4^2 + 4 = 20$$
$$f(20) = 9 - 20 = \textcircled{-11}$$

12.  $h(f(-6))$

$$f(-6) = 9 - (-6) = 15$$
$$h(15) = 15 - 2 = \textcircled{13}$$

13.  $f(h(-3))$

$$h(-3) = -3 - 2 = -5$$
$$f(-5) = 9 - (-5) = \textcircled{14}$$

14.  $h(g(11))$

$$g(11) = 11^2 + 11 = 132$$
$$h(132) = 132 - 2 = \textcircled{130}$$

15.  $g(h(-9))$

$$h(-9) = -9 - 2 = -11$$
$$g(-11) = (-11)^2 + (-11)$$
$$= \textcircled{110}$$

The given coordinates are on  $f(x)$ , find the coordinates for  $f^{-1}(x)$

1.  $(-2, 4)$

$$\textcircled{(4, -2)}$$

2.  $(4, 7)$

$$\textcircled{(7, 4)}$$

3.  $(0, 11)$

$$\textcircled{(11, 0)}$$

4.  $(-3, -8)$

$$(-8, -3)$$

5.  $(10, 10)$

$$(10, 10)$$

Find the algebraic inverse.

7.  $f(x) = 15x - 1$

$$y = 15x - 1$$

$$x = 15y - 1$$

$$x + 1 = 15y$$

$$\frac{x+1}{15} = y$$

8.  $f(x) = \frac{1}{3}x + 7$

$$y = \frac{1}{3}x + 7$$

$$x = \frac{1}{3}y + 7$$

$$x - 7 = \frac{1}{3}y$$

$$3(x - 7) = y$$

9.  $f(x) = -5x - 11$

$$y = -5x - 11$$

$$x = -5y - 11$$

$$x + 11 = -5y$$

$$\frac{x+11}{-5} = y$$

10.  $f(x) = (x-2)^2$   
 $y = (x-2)^2$   
 $x = (y-2)^2$   
 $\sqrt{x} = y-2$   
 $\sqrt{x} + 2 = y$

11.  $f(x) = \sqrt{x-4}$   
 $y = \sqrt{x-4}$   
 $x = \sqrt{y-4}$   
 $x^2 = y-4$   
 $x^2 + 4 = y$

Graph the function and its inverse of the given function.

12.

Function

Points

$(-2, -4)$

$(0, 1)$

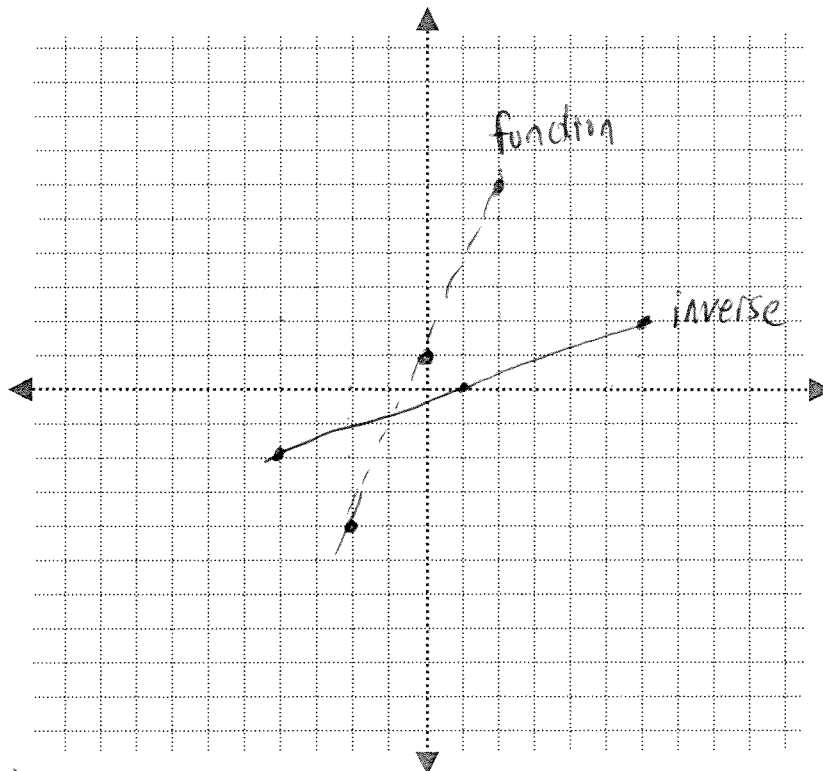
$(2, 6)$

Inverse

Points

$(-4, -2)$

$(1, 0)$   $(6, 2)$



13.

Function Points

$(4, 2)$

$(2, -2)$

$(-1, -5)$

$(-3, -7)$

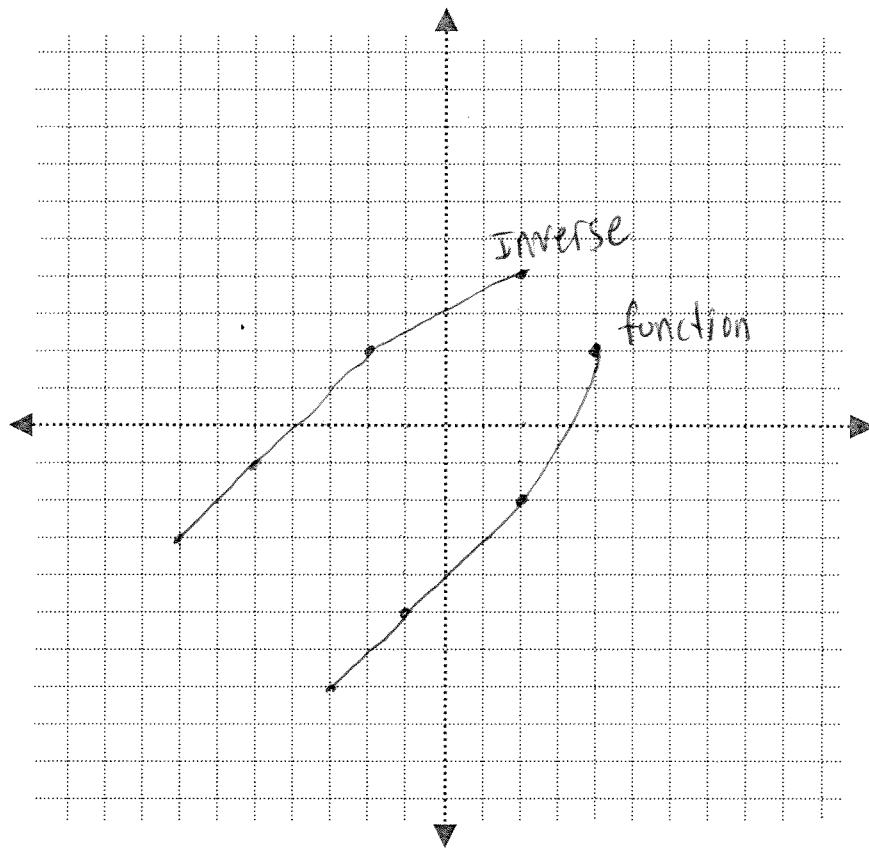
Inverse Points

$(2, 4)$

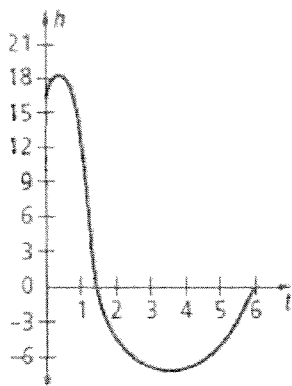
$(-2, 2)$

$(-5, -1)$

$(-7, -3)$



14. a. Does the graph pictured represent a function? Explain.



Yes, each  $x$ -value (input) has only one output. It passes the vertical line test.

b. Is the graph invertible? Explain.

No, it fails the horizontal line test. Each  $y$ -value has more than one  $x$ -value.

Station 2: Rational Functions

For each of the rational functions find: a. holes b. vertical asymptotes c. horizontal asymptotes  
d. zeros

$$1. f(x) = \frac{x^2 + x - 2}{x^2 - x - 6} = \frac{\cancel{(x+2)}(x-1)}{(x-3)\cancel{(x+2)}}$$

hole:  $x = -2$  zero:  $x = 1$

VA:  $x = 3$

HA:  $y = 1$

$$3. f(x) = \frac{3}{x-2}$$

hole: none

zero: none

VA:  $x = 2$

HA:  $y = 0$

$$4. f(x) = \frac{2x-1}{x}$$

hole: none

zero:  $x = \frac{1}{2}$

VA:  $x = 0$

HA:  $y = 2$

$$2. f(x) = \frac{2x^2}{x^2-1} = \frac{2x^2}{(x+1)(x-1)}$$

hole: ~~none~~ none

zero:  $x = 0$

VA:  $x = -1, x = 1$

HA:  $y = 2$

$$5. f(x) = \frac{x^2 + x - 12}{x^2 - 9} = \frac{\cancel{(x+4)}\cancel{(x-3)}}{\cancel{(x-3)}(x+3)}$$

hole:  $x = 3$

VA:  $x = -3$

HA:  $y = 1$

zero:  $x = -4$

$$6. f(x) = \frac{x^2 - 4}{x + 3} = \frac{(x+2)(x-2)}{x+3}$$

hole: none

zero:  $x = -2, x = 2$

VA:  $x = -3$

HA: none

$$7. f(x) = \frac{x^2 - x}{x+1} = \frac{x(x-1)}{x+1}$$

hole: none

VA:  $x = -1$

HA: none

Zero:  $x = 0, x = 1$

$$8. f(x) = \frac{x^2 - x - 2}{x-1} = \frac{(x-2)(x+1)}{x-1}$$

hole: none

VA:  $x = 1$

HA: none

Zero:  $x = 2, x = -1$

$$9. f(x) = \frac{x+1}{x^2+3x+2} = \frac{\cancel{x+1}}{(x+2)(\cancel{x+1})}$$

hole: ~~none~~  $x = -1$

VA:  $x = -2$

HA:  $y = 0$

zero: none

Simplify each expression.

$$1. \frac{x-4}{3} + \frac{5x}{3} = \frac{x-4+5x}{3} = \frac{6x-4}{3}$$

same  
denominator

$$4. \frac{3x-8}{4x} + \frac{-x+8}{4x} = \frac{3x-8-x+8}{4x}$$

$$= \frac{2x}{4x} = \frac{1}{2}$$

$$10. f(x) = \frac{x^2-9}{x^2-2x-3} = \frac{(x+3)(\cancel{x-3})}{(\cancel{x-3})(x+1)}$$

hole:  $x = 3$

VA:  $x = -1$

HA:  $y = 1$

zero:  $x = -3$

$$26. \frac{5x-3}{4x} - \frac{1}{6x} = \frac{6x(5x-3)}{(6x)4x} - \frac{(4x)1}{(4x)6x}$$

$$= \frac{30x^2 - 18x}{24x^2} - \frac{4x}{24x^2}$$

$$= \frac{30x^2 - 22x}{24x^2}$$

$$= \frac{2x(15x-11)}{24x^2}$$

$$= \boxed{\frac{15x-11}{12x}}$$

**Station 3: Composite Functions and Others**

1. Let  $C$  be the function that assigns to a temperature given in degrees Fahrenheit its equivalent in degrees Celsius, and let  $K$  be the function that assigns to a temperature given in degrees Celsius its equivalent in degrees Kelvin.

We have  $C(x) = \frac{5}{9}(x - 32)$  and  $K(x) = x + 273$ .

- a. Write an expression for  $K(C(x))$  and interpret its meaning in terms of temperatures.

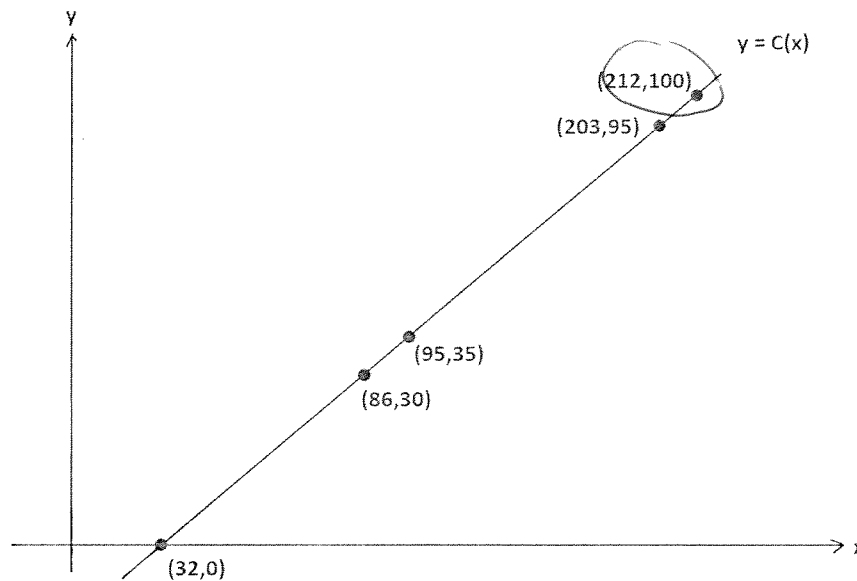
$$K\left(\frac{5}{9}(x-32)\right) = \frac{5}{9}(x-32) + 273$$

$\begin{matrix} C(x) & & K(x) \\ \text{°F} \rightarrow \text{°C} & & \text{°C} \rightarrow \text{K} \end{matrix}$

This function converts °F into Kelvin.

- b. The following shows the graph of  $y = C(x)$ .

According to the graph, what is the value of  $C^{-1}(100)$ ?  $C^{-1}(100) = 212$



$$C(x)$$

$$\text{°F} \rightarrow \text{°C}$$

$$C^{-1}$$

$$\text{°C} \rightarrow \text{°F}$$

- c. What does  $C^{-1}(100)$  mean in the context of this situation?

~~100~~ A temperature of  $100^{\circ}\text{C}$  is equivalent to  $212^{\circ}\text{F}$ .

- d. What does  $K^{-1}(273)$  mean in the context of this situation?

$$K(x) \quad K^{-1}(x)$$

$$\text{°C} \rightarrow \text{K} \quad \text{K} \rightarrow \text{°C}$$

A temperature of 273 Kelvin will be converted into °C.

